## **Constructing a Square the Ancient Indian Way Activity**

#### Overview

In this activity, the students will model constructing a square with a method similar to one the ancient Indians used in building a fire altar. The activity works best with the students working in pairs.

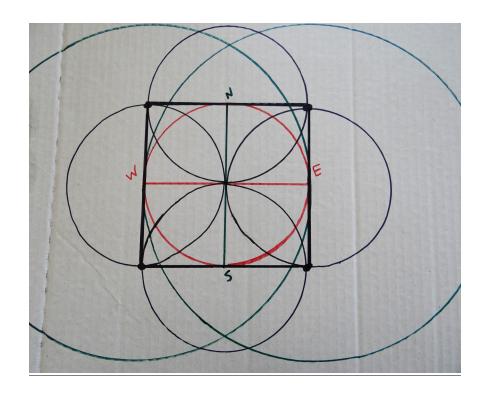
#### Materials for each pair of students

- 4 thumbtacks or push pins
- Square or rectangular piece of corrugated cardboard, e.g. the top of a pizza box
- Piece of string, length should be about half the length of the shortest side of the piece of cardboard, e.g. 7 inches for a 14 inch pizza box
- Straightedge
- Marker or pen

### Instructions

- 1. Tie a loop at each end of the string. (Instructions for tying a perfection loop knot can be found at <a href="http://www.netknots.com/fishing">http://www.netknots.com/fishing</a> knots/perfection-loop/ .)
- 2. Fold the string in half, and using the marker, mark the midpoint of the string.
- 3. Lay the string horizontally across the middle of the cardboard and trace a line segment with length the same as the string. This will be the East-West line. Then place a pushpin at the midpoint of the string, but not going through the string.
- 4. Remove the pushpin, place both loops on the shank of the pin, and replace the pin in the hole in the cardboard. Using the string like a compass, draw a circle in the cardboard.
- 5. Place pushpins at the East and West poles, the ends of the drawn diameter of the circle.
- 6. Put one loop of the string on the shank of the East pin and use the string to draw a circle with center at the East pin.
- 7. Repeat Step 6 at the West pin.
- 8. Draw the diameter of the first circle (from Step 4) which lies on the line connecting the points of intersection of the circles drawn in Steps 6 and 7. Place pushpins at the ends of this diameter (North and South poles).
- 9. At each of the 4 poles (East, South, West, and North), place both loops of the string on the shank of the pin and draw a circle.
- 10. The 4 (non-tangent) intersection points of the circles drawn in Step 9 are the four corners of the desired square.

# <u>Picture of a</u> Completed Activity



## Follow-up Activity

Have the students prove that the result is actually a square, by

- first proving it is a rhombus (hint: each side is the diameter of a congruent circle), and
- then proving that each interior angle is a right angle (hint: steps 6 8 construct a perpendicular bisector of the East-West line and each side of the "desired square" is tangent to the first circle from Step 4).

#### Notes

- The string should not be stretchy.
- Loops on the ends of the string should be fixed so they won't slide.
- When making circles, the pin should be held steady but not flush against the cardboard so that the loops can move freely about the shank of the pin.
- Watch out for the sharp ends of the pins poking through the cardboard.
- It is okay if the two larger circles from Steps 6 and 7 don't fit entirely on the cardboard, just as long as their two points of intersection are on the cardboard.
- <u>Common Core Standard G.CO.12</u> recommends making formal geometric constructions with a variety of tools and methods.
- This activity is included in the article, "Ancient Indian Rope Geometry in the Classroom," by Dr. Cynthia Huffman and Dr. Scott Thuong, in <u>MAA Convergence</u> (October 2015). The activity follows closely pp. 388-389 of Chapter 4, "Mathematics in India," by Kim Plofker, of *The Mathematics of Egypt, Mesopotamia, China, India, and Islam: A Sourcebook*, edited by Victor J. Katz and published by Princeton University Press in 2007.