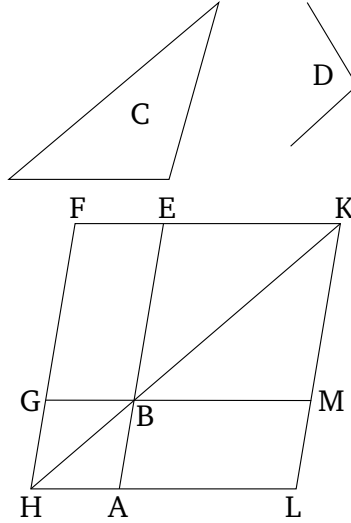


# Book 1

## Proposition 44

To apply a parallelogram equal to a given triangle to a given straight-line in a given rectilinear angle.



Let  $AB$  be the given straight-line,  $C$  the given triangle, and  $D$  the given rectilinear angle. So it is required to apply a parallelogram equal to the given triangle  $C$  to the given straight-line  $AB$  in an angle equal to (angle)  $D$ .

Let the parallelogram  $BEFG$ , equal to the triangle  $C$ , have been constructed in the angle  $EBG$ , which is equal to  $D$  [Prop. 1.42]. And let it have been placed so that  $BE$  is straight-on to  $AB$ .<sup>†</sup> And let  $FG$  have been drawn through to  $H$ , and let  $AH$  have been drawn through  $A$  parallel to either of  $BG$  or  $EF$  [Prop. 1.31], and let  $HB$  have been joined. And since the straight-line  $HF$  falls across the parallels  $AH$  and  $EF$ , the (sum of the) angles  $AHF$  and  $HFE$  is thus equal to two right-angles

[Prop. 1.29]. Thus, (the sum of)  $BHG$  and  $GFE$  is less than two right-angles. And (straight-lines) produced to infinity from (internal angles whose sum is) less than two right-angles meet together [Post. 5]. Thus, being produced,  $HB$  and  $FE$  will meet together. Let them have been produced, and let them meet together at  $K$ . And let  $KL$  have been drawn through point  $K$  parallel to either of  $EA$  or  $FH$  [Prop. 1.31]. And let  $HA$  and  $GB$  have been produced to points  $L$  and  $M$  (respectively). Thus,  $HLKF$  is a parallelogram, and  $HK$  its diagonal. And  $AG$  and  $ME$  (are) parallelograms, and  $LB$  and  $BF$  the so-called complements, about  $HK$ . Thus,  $LB$  is equal to  $BF$  [Prop. 1.43]. But,  $BF$  is equal to triangle  $C$ . Thus,  $LB$  is also equal to  $C$ . Also, since angle  $GBE$  is equal to  $ABM$  [Prop. 1.15], but  $GBE$  is equal to  $D$ ,  $ABM$  is thus also equal to angle  $D$ .

Thus, the parallelogram  $LB$ , equal to the given triangle  $C$ , has been applied to the given straight-line  $AB$  in the angle  $ABM$ , which is equal to  $D$ . (Which is) the very thing it was required to do.