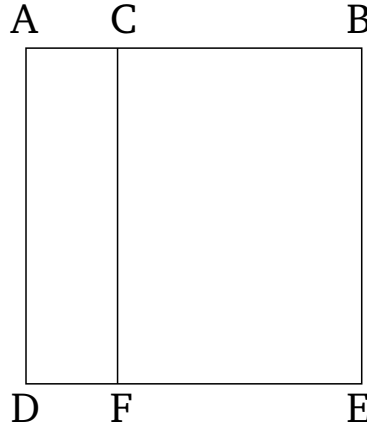


## Book 2

### Proposition 2

If a straight-line is cut at random then the (sum of the) rectangle(s) contained by the whole (straight-line), and each of the pieces (of the straight-line), is equal to the square on the whole.



For let the straight-line  $AB$  have been cut, at random, at point  $C$ . I say that the rectangle contained by  $AB$  and  $BC$ , plus the rectangle contained by  $BA$  and  $AC$ , is equal to the square on  $AB$ .

For let the square  $ADEB$  have been described on  $AB$  [Prop. 1.46], and let  $CF$  have been drawn through  $C$ , parallel to either of  $AD$  or  $BE$  [Prop. 1.31].

So the (square)  $AE$  is equal to the (rectangles)  $AF$  and  $CE$ . And  $AE$  is the square on  $AB$ . And  $AF$  (is) the rectangle contained by the (straight-lines)  $BA$  and  $AC$ . For it is contained by  $DA$  and  $AC$ , and  $AD$  (is) equal to  $AB$ . And  $CE$  (is) the (rectangle contained) by  $AB$  and  $BC$ . For  $BE$  (is) equal to  $AB$ . Thus, the (rectangle contained) by  $BA$  and  $AC$ , plus the (rectangle contained) by  $AB$  and  $BC$ , is equal to the square on  $AB$ .

Thus, if a straight-line is cut at random then the (sum of the) rectangle(s) contained by the whole (straight-line), and each of the pieces (of the straight-line), is equal to the square on the whole. (Which is) the very thing it was required to show.