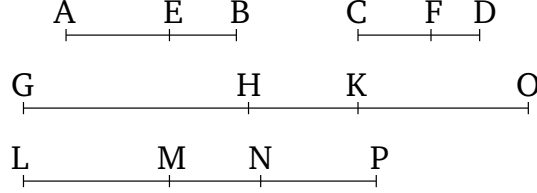


## Book 5

### Proposition 17

If composed magnitudes are proportional then they will also be proportional (when) separated.



Let  $AB$ ,  $BE$ ,  $CD$ , and  $DF$  be composed magnitudes (which are) proportional, (so that) as  $AB$  (is) to  $BE$ , so  $CD$  (is) to  $DF$ . I say that they will also be proportional (when) separated, (so that) as  $AE$  (is) to  $EB$ , so  $CF$  (is) to  $DF$ .

For let the equal multiples  $GH$ ,  $HK$ ,  $LM$ , and  $MN$  have been taken of  $AE$ ,  $EB$ ,  $CF$ , and  $FD$  (respectively), and the other random equal multiples  $KO$  and  $NP$  of  $EB$  and  $FD$  (respectively).

And since  $GH$  and  $HK$  are equal multiples of  $AE$  and  $EB$  (respectively),  $GH$  and  $GK$  are thus equal multiples of  $AE$  and  $AB$  (respectively) [Prop. 5.1]. But  $GH$  and  $LM$  are equal multiples of  $AE$  and  $CF$  (respectively). Thus,  $GK$  and  $LM$  are equal multiples of  $AB$  and  $CF$  (respectively). Again, since  $LM$  and  $MN$  are equal multiples of  $CF$  and  $FD$  (respectively),  $LM$  and  $LN$  are thus equal multiples of  $CF$  and  $CD$  (respectively) [Prop. 5.1]. And  $LM$  and  $GK$  were equal multiples of  $CF$  and  $AB$  (respectively). Thus,  $GK$  and  $LN$  are equal multiples of  $AB$  and  $CD$  (respectively). Thus,  $GK$ ,  $LN$  are equal multiples of  $AB$ ,  $CD$ . Again, since  $HK$  and  $MN$  are equal multiples of  $EB$  and  $FD$

(respectively), and  $KO$  and  $NP$  are also equal multiples of  $EB$  and  $FD$  (respectively), then, added together,  $HO$  and  $MP$  are also equal multiples of  $EB$  and  $FD$  (respectively) [Prop. 5.2]. And since as  $AB$  (is) to  $BE$ , so  $CD$  (is) to  $DF$ , and the equal multiples  $GK$ ,  $LN$  have been taken of  $AB$ ,  $CD$ , and the equal multiples  $HO$ ,  $MP$  of  $EB$ ,  $FD$ , thus if  $GK$  exceeds  $HO$  then  $LN$  also exceeds  $MP$ , and if ( $GK$  is) equal (to  $HO$  then  $LN$  is also) equal (to  $MP$ ), and if ( $GK$  is) less (than  $HO$  then  $LN$  is also) less (than  $MP$ ) [Def. 5.5]. So let  $GK$  exceed  $HO$ , and thus,  $HK$  being taken away from both,  $GH$  exceeds  $KO$ . But (we saw that) if  $GK$  was exceeding  $HO$  then  $LN$  was also exceeding  $MP$ . Thus,  $LN$  also exceeds  $MP$ , and,  $MN$  being taken away from both,  $LM$  also exceeds  $NP$ . Hence, if  $GH$  exceeds  $KO$  then  $LM$  also exceeds  $NP$ . So, similarly, we can show that even if  $GH$  is equal to  $KO$  then  $LM$  will also be equal to  $NP$ , and even if ( $GH$  is) less (than  $KO$  then  $LM$  will also be) less (than  $NP$ ). And  $GH$ ,  $LM$  are equal multiples of  $AE$ ,  $CF$ , and  $KO$ ,  $NP$  other random equal multiples of  $EB$ ,  $FD$ . Thus, as  $AE$  is to  $EB$ , so  $CF$  (is) to  $FD$  [Def. 5.5].

Thus, if composed magnitudes are proportional then they will also be proportional (when) separated. (Which is) the very thing it was required to show.