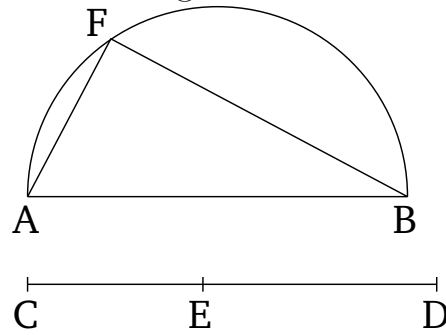


# Book 10

## Proposition 30

To find two rational (straight-lines which are) commensurable in square only, such that the square on the greater is larger than the (the square on) lesser by the (square) on (some straight-line which is) incommensurable in length with the greater.



Let the rational (straight-line)  $AB$  be laid out, and the two square numbers,  $CE$  and  $ED$ , such that the sum of them,  $CD$ , is not square [Prop. 10.28 lem. II]. And let the semi-circle  $AFB$  have been drawn on  $AB$ . And let it be contrived that as  $DC$  (is) to  $CE$ , so the (square) on  $BA$  (is) to the (square) on  $AF$  [Prop. 10.6 corr]. And let  $FB$  have been joined.

So, similarly to the (proposition) before this, we can show that  $BA$  and  $AF$  are rational (straight-lines which are) commensurable in square only. And since as  $DC$  is to  $CE$ , so the (square) on  $BA$  (is) to the (square) on  $AF$ , thus, via conversion, as  $CD$  (is) to  $DE$ , so the (square) on  $AB$  (is) to the (square) on  $BF$  [Props. 5.19 corr., 3.31, 1.47]. And  $CD$  does not have to  $DE$  the ratio which (some) square number (has) to (some) square number. Thus, the (square) on  $AB$  does not have to the (square) on

$BF$  the ratio which (some) square number has to (some) square number either. Thus,  $AB$  is incommensurable in length with  $BF$  [Prop. 10.9]. And the square on  $AB$  is greater than the (square on)  $AF$  by the (square) on  $FB$  [Prop. 1.47], (which is) incommensurable (in length) with  $(AB)$ .

Thus,  $AB$  and  $AF$  are rational (straight-lines which are) commensurable in square only, and the square on  $AB$  is greater than (the square on)  $AF$  by the (square) on  $FB$ , (which is) incommensurable (in length) with  $(AB)$ .<sup>†</sup> (Which is) the very thing it was required to show.